

LIST OF FORMULAE IN MATHS FOR CLASS X

CHAPTER-1 REAL NUMBERS (6 Marks)

1. Euclid's division lemma: Given positive integers a and b, there exists unique integers q and r satisfying $a = bq + r$, $0 \leq r < b$.
2. Fundamental theorem of Arithmetic: Every composite number can be expressed as a product of primes.
3. In rational number $\frac{p}{q}$, q is always in form of $2^n 5^m$ (for terminating decimal representation).
4. $\text{HCF}(a,b) \times \text{LCM}(a,b) = a \times b$.

CHAPTER-2 POLYNOMIALS (4 Marks)

5. Zeroes of a polynomial: k is zero of polynomial P(x) if $P(k) = 0$.
6. Sum of zeroes $\alpha + \beta = -\frac{b}{a}$, product of zeroes $\alpha \times \beta = \frac{c}{a}$ for polynomial $ax^2 + bx + c = k[x^2 - (\alpha + \beta)x + \alpha\beta]$
7. For cubic polynomial, $ax^3 + bx^2 + cx + d$ $\alpha + \beta + \gamma = -\frac{b}{a}$, $\alpha\beta + \beta\gamma + \gamma\alpha = \frac{c}{a}$, $\alpha\beta\gamma = -\frac{d}{a}$

CHAPTER-3 PAIR OF LINEAR EQUATIONS IN TWO VARIABLES (6 Marks)

8. For $a_1x + b_1y + c_1 = 0$ and For $a_2x + b_2y + c_2 = 0$,
unique solution: $\frac{a_1}{a_2} \neq \frac{b_1}{b_2}$ graph: two intersecting lines
no solution: $\frac{a_1}{a_2} = \frac{b_1}{b_2} \neq \frac{c_1}{c_2}$ parallel lines
infinite solution: $\frac{a_1}{a_2} = \frac{b_1}{b_2} = \frac{c_1}{c_2}$ coincident lines
9. Elimination method to solve equations
10. Cross multiplication rule: $a_1x + b_1y + c_1 = 0$ and $a_2x + b_2y + c_2 = 0$ then $x = \frac{(b_1c_2 - b_2c_1)}{a_1b_2 - a_2b_1}$ and $y = \frac{(c_1a_2 - c_2a_1)}{a_1b_2 - a_2b_1}$

CHAPTER-4 QUADRATIC EQUATIONS (6 Marks)

11. $ax^2 + bx + c = 0$ root are real if $D = b^2 - 4ac \geq 0$
roots are equal if $D = b^2 - 4ac = 0$, $x = \frac{-b \pm \sqrt{D}}{2a}$

CHAPTER-5 ARITHMETIC PROGRESSIONS (4 Marks)

12. General term of the A.P. $a_n = a + (n-1)d$ where a=first term, d = common difference
13. Sum of n terms of an A.P. $S_n = \frac{n}{2}[2a + (n-1)d] = \frac{n}{2}[a + l]$
14. Sequence of A.P. is : a, a+d, a+2d,

CHAPTER-6 SIMILAR TRIANGLES (6 Marks)

15. Similarity rules of two triangles: (i) SSS (ii) SAS (iii) AA
16. Theorem: (i) The ratio of the areas of two similar triangles is equal to the squares of the ratio of their corresponding sides.
17. (ii) [BPT] If a line is drawn parallel to one side of a triangle, it cuts other two sides in the same ratio.
18. (iii) Pythagoras theorem: In right triangle, the square of the hypotenuse is equal to the sum of the squares of the other two sides.

(iv) Converse of Pythagoras theorem : In a triangle , if square of one side is equal to the sum of the squares of the other two sides , then the angle opposite the first side is a right angle

CHAPTER-7 COORDINATE GEOMETRY (6 Marks)

19. The distance between P(x₁,y₁) and Q(x₂,y₂) is $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$
20. The distance of point P(x,y) from the origin is $\sqrt{x^2 + y^2}$
21. The coordinates of the point P(x,y) which divides the line segment joining the points A(x₁,y₁) and B(x₂,y₂) internally in the ratio m₁:m₂ are $\left(\frac{m_1x_2+m_2x_1}{m_1+m_2}, \frac{m_1y_2+m_2y_1}{m_1+m_2}\right)$.
22. The mid-point of the line segment joining the points P(x₁,y₁) and Q(x₂,y₂) is $\left(\frac{x_1+x_2}{2}, \frac{y_1+y_2}{2}\right)$.
23. The area of the triangle formed by the points (x₁,y₁), (x₂,y₂) and (x₃,y₃) is the numerical value of the expression $\frac{1}{2}[x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$

CHAPTER-8 INTRODUCTION TO TRIGONOMETRY (8 Marks)

	0°	30°	45°	60°	90°
Sin A	0	$\frac{1}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1
Cos A	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0

24. $\sin A = \frac{P}{H}$, $\cos A = \frac{B}{H}$, $\tan A = \frac{P}{B}$, $\cot A = \frac{1}{\tan A}$, $\sec A = \frac{1}{\cos A}$, $\operatorname{cosec} A = \frac{1}{\sin A}$
25. $\sin(90^\circ - A) = \cos A$, $\cos(90^\circ - A) = \sin A$, $\tan(90^\circ - A) = \cot A$, $\cot(90^\circ - A) = \tan A$, $\sec(90^\circ - A) = \operatorname{cosec} A$, $\operatorname{cosec}(90^\circ - A) = \sec A$,
26. $\sin^2 A + \cos^2 A = 1$, $\sec^2 A - \tan^2 A = 1$ for $0^\circ \leq A \leq 90^\circ$, $\operatorname{cosec}^2 A = 1 + \cot^2 A$ for $0^\circ < A \leq 90^\circ$.

CHAPTER- 9 SOME APPLICATION OF TRIGONOMETRY (4 Marks)

27. **Angle of Elevation:** When the object is above the eye then the **angle of elevation** of an object as seen by an observer is the angle between the horizontal and the line from the object to the observer's eye (the line of sight).
28. **Angle of Depression:** When the object is below the eye then angle between the horizontal and the observer's line of sight is called the **angle of depression**.

CHAPTER-10 CIRCLES (5 Marks)

29. Theorems (i) The tangent at any point of a circle is perpendicular to the radius through the point of contact. (ii) The length of tangents drawn from an external point to a circle are equal.

CHAPTER-11 CONSTRUCTIONS of similar triangles and construction of Tangents to a circle. (4 Marks)

CHAPTER-12 AREA RELATED TO CIRCLE (4 Marks) (i) Area of the sector = $\frac{\theta}{360^\circ} \pi r^2$

(ii) length of arc = $\frac{\theta}{360^\circ} 2\pi r$ (iii) Area of minor segment = $\frac{\theta}{360^\circ} \pi r^2 - \frac{1}{2} r^2 \sin \theta$.

CHAPTER-13 SURFACE AREAS AND VOLUME (6 Marks)

Object	CSA	TSA	Volume
Cube	4a ²	6a ²	a ³
Cuboid	2h(l+b)	2(lb +bh + hl)	lbh
Cylinder	2πrh	2πrh + 2πr ²	πr ² h

Cone	$\pi r l$	$\pi r l + \pi r^2$	$\frac{1}{3} \pi r^2 h$
Sphere	-	$4\pi r^2$	$\frac{4}{3} \pi r^3$
Hemisphere	$2\pi r^2$	$3\pi r^2$	$\frac{2}{3} \pi r^3$

- (i) Volume of a frustum of cone = $\frac{1}{3} \pi h (r_1^2 + r_2^2 + r_1 r_2)$.
- (ii) Curved surface area of a frustum of cone = $\pi l (r_1 + r_2)$ where $l = \sqrt{h^2 + (r_1 - r_2)^2}$.
- (iii) Total surface area of frustum of cone = $\pi l (r_1 + r_2) + \pi (r_1^2 + r_2^2)$

CHAPTER-14 STATISTICS (7 Marks)

A. Mean

- (i) The direct method: $\bar{x} = \frac{\sum f_i x_i}{\sum f_i}$ (iii) The assumed mean method: $\bar{x} = a + \frac{\sum f_i d_i}{\sum f_i}$
- (ii) The step deviation method: $\bar{x} = a + \left(\frac{\sum f_i u_i}{\sum f_i} \right) \times h$

B. Mode = $l + \left(\frac{f_1 - f_0}{2f_1 - f_0 - f_2} \right) \times h$

Where l = lower limit of the modal class,
 h = size of the class interval (assuming all class sizes to be equal).
 f_1 = frequency of the modal class,
 f_2 = frequency of the class succeeding the modal class,
 f_0 = frequency of the class preceding the modal class.

C. Median = $l + \left(\frac{\frac{n}{2} - cf}{f} \right) \times h$

l = lower limit of median class,
 n = number of observations,
 cf = cumulative frequency of class preceding the median class,
 f = frequency of median class,
 h = class size (assuming class size to be equal).

*** Mode = 3Median - 2Mean**

*** More than ogive : plot points (lower limit , corresponding cumulative frequency)**

*** Less than ogive : plot points (upper limit , corresponding cumulative frequency)**

CHAPTER-15 PROBABILITY (4 Marks)

$$P(E) = \frac{\text{Number of outcomes favourable to } E}{\text{Number of all possible outcomes of experiment}}$$

Sum of probabilities of all events is always 1 in an experiment, $0 \leq P(E) \leq 1$, $P(E) + P(\text{Not } E) = 1$